

Name: \_\_\_\_\_

Student Number: \_\_\_\_\_

**You MUST show your work and give reasons for your answers!**  
**Good luck.**

(1) Find the interval and radius of convergence for the power series

$$\sum_{n=0}^{n=\infty} (-1)^n \frac{x^n}{n\sqrt{n}}$$

- (2) Find the power series for the function  $f(x) = \ln(x + 1)$  centered at  $a = 0$ . What is its radius of convergence?

(3) Given that  $\sin(x) = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!}$  find a power series for  $\frac{\sin(x)}{x}$  and use it to evaluate  $\int_0^{1/10} \frac{\sin(x)}{x}$  with an error less than  $10^{-6}$ .

(4) Test the series for convergence:  
(a)  $\sum_{n=0}^{\infty} (-1)^n \frac{n}{n+1}$

(b)  $\sum_{n=0}^{n=\infty} \frac{\arctan(n)}{n^2+1}$

(5) Find the limit of the sequence  $a_n = \frac{\ln(n)}{n}$ .

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(1) Find the interval and radius of convergence for the power series

$$\sum_{n=2}^{n=\infty} (-1)^n \frac{x^n}{\ln(n)}$$

- (2) Find the power series for the function  $f(x) = \arctan(x)$  centered at  $a = 0$ . What is its radius of convergence?

- (3) Given that  $\cos(x) = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!}$  find a power series for  $x^2 \cos(x)$  and use it to evaluate  $\int_0^{1/10} x^2 \cos(x) dx$  with an error less than  $10^{-6}$ .

- (4) Test the series for convergence:  
(a)  $\sum_{n=0}^{\infty} (-1)^n \arctan(n)$

(b)  $\sum_{n=0}^{n=\infty} \frac{\ln(n)}{n}$

(5) Find the limit of the sequence  $a_n = \sqrt{\frac{n^2+5}{3n^2-7}}$ .