

**SPRING 2008 — MA 227 — TEST 4**  
**APRIL 21, 2008**

Name: \_\_\_\_\_

1. PART I

There are 6 problems in Part 1, each worth 4 points. Place your answer on the line to the right of the question. Only your answer on the answer line will be graded.

- (1) Compute  $\operatorname{div} \mathbf{F}$  when  $\mathbf{F}(x, y, z) = \langle \sin(xz), e^{xy}, yz \rangle$ .

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- (2) Find the curl of the vector field  $\mathbf{F}(x, y, z) = \langle xyz, \sin(xz), z \rangle$ .

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- (3) Compute  $\nabla f$  when  $f = 2x^2 - xy + z^2$ .

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- (4) Argue if the vector field  $F(x, y) = \langle 2x, -xy \rangle$  is conservative.

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- (5) Find a function  $f$  such that  $\nabla f = \langle 4xy^{\frac{5}{2}}, 5x^2y^{\frac{3}{2}} \rangle$ .

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- (6) Evaluate the line integral  $\int_C 3ds$  where  $C$  is a segment of the straight line connecting the points  $(-1,1)$  and  $(1,3)$ .
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## 2. PART II

There are 3 problems in Part 2, each worth 12 points. On Part 2 problems partial credit is awarded where appropriate. Your solution must include enough detail to justify any conclusions you reach in answering the question.

- (1) Let  $C$  be the boundary of the unit square (with vertices at  $(0,0)$ ,  $(1,0)$ ,  $(1,1)$ , and  $(0,1)$ ) oriented counterclockwise. Evaluate

$$\int_C (y^2 dx - xy dy)$$

by two methods: directly as a line integral and using Green's Theorem.

- (2) Find the work done by the force field  $\mathbf{F} = 2x \mathbf{i} + 3y \mathbf{j}$  on a particle that moves along a line segment from the point  $(1, 1)$  to the point  $(3, 5)$ .

- (3) Find the surface area of that part of the surface  $\mathbf{r}(u, v) = \langle u, u + 2v, v^2 \rangle$  where  $0 \leq u \leq 2$ ,  $0 \leq v \leq 1$ .