Department of Mathematics, UAB
Mathematics of Biological Systems I
MA 168-VT Spring 2023

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Class Meetings: MTuWTh: 12:20–13:10, HHB221.
Office Hours. After class; email me for additional office or Zoom meetings.
Texts. *Modeling Life* by Alan Garfinkel, Jane Shevetsov, and Yina Guo, Springer International Publishing AG 2017. My lecture notes; download these from Canvas.
Prerequisite Course. MA168 or MA125, or MA225.
Term Dates. First day of classes: Mon Jan 09, 2023. Spring Break: Mar 13–19. Last day of classes: Friday April 21, 2023.

SageMath Software. Access to the SageMath software package is needed for this course. This package may be freely downloaded from the SageMath website `https://www.sagemath.org/` (this is a "live" URL), with available binaries for Mac, Linux, and Windows that may be obtained by clicking the download button Download 9.7 on this website. The Mac machines in HHB221 have version 9.4 of SageMath already installed for use during class. SageMath is a computer algebra system with features covering many aspects of mathematics, including calculus, statistics, numerical analysis, algebra, combinatorics, graph theory, and number theory, Together with the web-browser-based Jupyter Notebook this software contains much of the functionality of the commercial packages Mathematica, Maple, and Matlab and uses a similar command set to the popular programming language Python whose syntax you will naturally acquire as you use SageMath. Please note that you will develop the necessary programming skills during the course, and no prior computer skills are assumed at the beginning of the course.

Syllabus. In the course we teach mathematical modeling as a tool for understanding how biological and physical systems evolve over time. We begin with models of dynamical processes occurring in ecology, biology, physiology, physics, biochemistry, neurology, and other areas involving the study of quantities that change with time. In the lab sessions, we will often run prepackaged computer programs for problem-solving, visualization, plotting and simulation. Basic programming concepts like program flow control and data structures will be introduced as needed.

As we proceed you will notice that the process of modeling involves rewriting real-world problems in mathematical terms so as to facilitate their solution. Inevitably, in pursuing these ends one must bump into the fundamentally powerful ideas, techniques, and notations of Calculus, but for us this will not happen right away. Rather, we use the model problems themselves to uncover the need to use Calculus, and thereby obtain a deeper understanding of both.

The overall focus of the course is to use the math to help us understand the science.

Aims of the Course. Upon successful completion of the course a student can

- describe the dynamics in practical systems and the different types of behaviors of complex systems including steady-states and oscillations, and their causes including the effects of delay, and positive and negative feedback;
- explain how the variables in each term in the differential equations arise from practical observations and assumptions;
- translate a verbal description of interacting variables into a differential equation model of a dynamical system, using the concepts of state space and tangent space;
- simulate differential equation models using Euler's method by hand, and on a computer using PYTHON and SAGEMATH;
- derive models of biological systems that exhibit bi-stability or switch-like behavior using the concept of positive feedback; use negative feedback to model the neuron as an excitable oscillatory dynamical system.

Grading. At the beginning of the term you will each be assigned to a study group containing four or so of your fellow students. The intention here is that you will work with your study group on homework (and lab) assignments, both inside and outside of class, prior to submitting each assignment individually on Canvas on or before the due time.

There will be approximately one homework assignment and one computer lab assignment per week; collectively the homework assignments and the labs will each constitute 20% of the course grade. The midterm and final exams will each count 30%. Each exam will consist of a group part, and an individual part, each counting 15%. For the group part you will work with your study group on a set of review problems that I will provide, and submit (**one** pdf file, on Canvas) the solutions as a group for grading during the week before each individual exam. The individual part will be an in-class exam based upon the review problems for that exam.

Your final grade is determined from your course grade according to the following table:

Course Grade:	88-100	75-87	62-74	50-61	below 50
Final Grade:	A	B	C	D	F

Lab/Homework File Submission. For each Homework assignment you are required to submit a **single** *.pdf file in Canvas on or before the due time. Paper homework sheets can be scanned to a single pdf file using a mobile scanning app such as Adobe Scan, for example.

Likewise, for each Lab assignment you need to submit a **single** *.pdf or *.ipynb or *.html file in Canvas on or before the due time.

Reference Material. The prescribed text, *Modeling Life* by Alan Garfinkel, Jane Shevetsov, and Yina Guo, Springer International Publishing (2017) is useful inter alia as a supplementary reference if you seek more than is in my lecture notes. There is no formal text for the Lab component of the course, which we will do as an in-class/homework activity. Regular class attendance, while not mandatory, is highly recommended for this reason. For SageMath and Python, the online documentation is quite good, but of course you should never hesitate to ask either me or KJ if your code is not behaving properly.

Class Schedule.

Week	**Monday**	**Wednesday**	**Thursday**
01/09 – 01/13	First Class/Lab 1		HW 1
01/16 – 09/20	Lab 2/Lab 1 due		HW2/HW1 due
01/23 – 01/27	Lab 3/Lab 2 due		HW3/HW2 due
02/06 – 02/10	Lab 4/Lab 3 due		HW4/HW3 due
02/13 – 02/17	Lab 5/Lab 4 due		HW5/HW4 due
02/20 – 02/24	Lab 6/Lab 5 due	Midterm Review	HW5 due
02/27 – 03/03	Lab 6 due	Midterm Review due	
03/06 – 03/10		Midterm Exam	HW6
03/13 – 03/17	Spring Break		
03/20 – 03/24	Lab 7		HW7/HW6 due
03/27 – 03/31	Lab 8/Lab 7 due		HW8/HW7 due
04/03 – 04/07	Lab 9/ Lab 8 due		HW8 due
04/10 – 04/14	Lab 9 due	Final Review	
04/17 – 04/21		Final Review due	Last Class
04/24 – 04/28		Final Exam 1:30–4	